# Contents

#### 1. Introduction 1

- 1–0. General 1
- 1–1. Equilibrium between Solid and Liquid 1
- 1–2. Melting Point 2
- 1–3. Equilibrium of Alloys 4

Equilibrium Diagrams4Congruent Melting6Eutectics6Peritectics7Monotectics10

- 1–4. Gas–Metal Equilibrium 11
- 1–5. Ternary and Multicomponent Alloys 12
- 1–6. The Phase Rule 14
- 1–7. The Distribution Coefficient 15
- 1–8. Thermodynamic Criteria for Equilibrium 17

#### 2. Solidification as an Atomic Process 20

2-1. Solids and Liquids 20

The Nature of Crystalline Solids20Nature of Liquids22The Differences Between Crystals and Liquids24Quasi-chemical Approach25

2–2. The Solid-Liquid Interface 26

Microtopography of the Interface 28

- 2-3. Equilibrium between a Pure Metal and Its Melt 352-4. The Process of Crystal Growth 43
  - Kinetics of Crystal Growth 44
    - ix

#### CONTENTS

2-5. Solid-Liquid Equilibrium in Alloys 462-6. Origin of Defects 51

Vacancies 52 Dislocations 56 Lineage Structures 59

#### 3. Nucleation 62

- 3-1. Metastability of Supercooled Liquids 62
- 3–2. Equilibrium Conditions for a Curved Interface 63

Stability of a Curved Interface; Atomic Considerations 63 Thermodynamic Treatment of Equilibrium across a Curved Interface 64

3–3. Calculation of Critical Radius 65

3–4. The Process of Nucleation 68

Theory of Nucleation Rate69Nucleation Temperature70Comparison between Experiment and Theory71Size of the Critical Nucleus74

- 3–5. Homogeneous Nucleation in Alloys 76
- 3–6. Heterogeneous Nucleation 77
- 3–7. The Nucleation of Melting 84
- 3–8. Dynamically Stimulated Nucleation 86
- 3-9. Summary of Present Status of Nucleation Theory 89
- 4. Microscopic Heat Flow Considerations 91
- 4–1. Qualitative Observations 91
- 4–2. Removal of Latent Heat 95
- 4-3. Extraction of Latent Heat by Conduction into the Crystal 96

Effect of Surfaces and of Grain Boundaries 97

4-4. Conduction of Latent Heat into the Liquid 99

"Ribbon" Crystals 101 "Feather" Growth 102

4–5. Dendritic Growth 103

Total Amount Solidified104Speed of Growth104

#### CONTENTS

Direction of Dendritic Growth 116 Spacing of Dendrite Arms 120

4–6. Solidification at Very High Supercooling 122

#### 5. Redistribution of Solute during Solidification 126

- 5–1. General Considerations 126
- 5–2. The Distribution Coefficient 126
- 5–3. Rejection of Solute 128

Equilibrium Maintained at All Times 129
Mixing in the Liquid by Diffusion Only: No Diffusion in the Solid 131
Influence of Fluid Motion: Convection 138
Complete or Partial Mixing of Liquid: No Diffusion in Solid 139
Solidus Temperature of an Alloy 142

- 5–4. Zone Refining 143
- 5–5. Constitutional Supercooling 150

Instability Due to Constitutional Supercooling 152

5–6. Cellular Substructure 154

Origin of the Cellular Substructure 154 Quantitative Studies of Cell Formation 157 Geometry of Cells 160

- 5–7. Cellular Dendrites 164
- 5–8. Free Dendritic Growth in Alloys 169

Spacing of Dendrite Arms 170

- 5-9. Nucleation of Crystals ahead of the Existing Interface 171 5-10. Types of Segregation 171
- 5-10. Types of Segregation 171

Normal Segregation171Grain Boundary Segregation172Cellular Segregation173Dendritic Segregation175Inverse Segregation178Coring and Intercrystalline Segregation183Gravity Segregation183

6.	Polyphase Solidification 186
6–1.	Evolution of a Gas During Solidification 186
	Gas–Metal Equilibrium 186 Bubble Formation 187 Formation of Compounds by Dissolved Gases 194
6–2.	Eutectics 194
	Microstructure of Eutectics 196 Pure Binary Eutectics 197 Solidification of Lamellar Eutectics 198 Shape of the Interface 200 Lamellar Growth: Theoretical 201 Lamellar Growth: Experimental 204 Degenerate Eutectic Structures 206 Modification of Eutectics 207 Discontinuous Eutectics 211 Noneutectic Compositions 215 Structure of Eutectic Liquids 216 Gravity Segregation of Eutectics 218 Divorced Eutectic 218 Ternary Eutectics 219 Cast Iron 219
6–3. 6–4.	Peritectic Solidification224Solidification in the Presence of a Solid Phase227
	Suspended Particles 227 Solidification of a Liquid in a Porous Solid 229
7.	Macroscopic Heat Flow and Fluid Flow 232
7–1. 7–2.	General Considerations 232 Fluid Flow 232
	Viscosity of Liquid Metals 233 Fluidity 234
7–3.	Heat Flow 235
	Rate of Solidification 237 Continuous Casting 242 Dip Forming 247

7-4. Thermal Stresses in a Solidifying Body 250

## CONTENTS

8.	The Structure of Cast Metals 253
8–1. 8–2.	General Considerations253The Macrostructure of Cast Metals255
	Description of Cast Structures 255 Experimental Observations 257 Solidification in a Mold 259 Structure of Continuous Castings 276 Effect of Vibration on Structure 278 Welding, Brazing and Soldering as Casting Processes 281
8-3.	Segregation 282
8–4. 8–5.	The Significance of Small-Scale Experiments284Change of Volume on Freezing285
	Pipe Formation 286 Unidirectional Shrinkage 287 Cavity Formation 287 Control of Unsoundness 287 Porosity 288 Surface Porosity 289
8–6. 8–7.	Blowholes 289 Surface Topography Resulting from Solidification 290
	Surface Tension Effects291Cold Shut292Trapped Gas292Surface Dendrites292Exudation and Surface Porosity294Topography of the Free Surface294Changes of Topography after Solidification294Metal Coating by Hot Dipping295Tinplate295
	Appendix. The Production of Single Crystals from the Melt 298
A–1.	General Considerations 298
A–2. A–3.	Control of Orientation 299 Control of Shape 300

A-4. Control of Composition 302

Contamination 302

### CONTENTS

Evaporation303Uniformity of Composition: Short Range303Uniformity of Composition: Long Range303Peritectic Compound305

A-5. Control of Perfection 305

Vacancies 305 Dislocations 306 Lineage 306 "Stray Crystals" 307

A-6. Bicrystals 308

Index 311

xiv