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# PHASE SPACE APPROACH TO SOLVING THE SCHRÖDINGER EQUATION: THINKING INSIDE THE BOX

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# THEORIES AND QUANTUM CHEMICAL CALCULATIONS OF LINEAR AND SUM-FREQUENCY GENERATION SPECTROSCOPIES, AND INTRAMOLECULAR VIBRATIONAL REDISTRIBUTION AND DENSITY MATRIX TREATMENT OF ULTRAFAST DYNAMICS

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# ON THE KRAMERS VERY LOW DAMPING ESCAPE RATE FOR POINT PARTICLES AND CLASSICAL SPINS

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