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# Generalized Axiomatic Scale-Space Theory

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# Smoothlet Transform: Theory and Applications

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# Theory and Computation of Electron Mirrors: The Central Particle Method

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