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# MULTIDIMENSIONAL INCOHERENT TIME-RESOLVED SPECTROSCOPY AND COMPLEX KINETICS

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# COMPLEX MULTICONFIGURATIONAL SELF-CONSISTENT FIELD-BASED METHODS TO INVESTIGATE ELECTRON-ATOM/MOLECULE SCATTERING RESONANCES

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# DETERMINATION OF MOLECULAR ORIENTATIONAL CORRELATIONS IN DISORDERED SYSTEMS FROM DIFFRACTION DATA

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# RECENT ADVANCES IN STUDYING MECHANICAL PROPERTIES OF DNA

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# VISCOELASTIC SUBDIFFUSION: GENERALIZED LANGEVIN EQUATION APPROACH

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# EFFICIENT AND UNBIASED SAMPLING OF BIOMOLECULAR SYSTEMS IN THE CANONICAL ENSEMBLE: A REVIEW OF SELF-GUIDED LANGEVIN DYNAMICS

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