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# THE DECOUPLING OF ELECTRONIC AND NUCLEAR MOTIONS IN THE ISOLATED MOLECULE SCHRÖDINGER HAMILTONIAN

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