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ON THE STATICS AND DYNAMICS OF MAGNETOANISOTROPIC NANOPARTICLES

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Acknowledgments

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RELAXATION TIMES FOR SINGLE-DOMAIN FERROMAGNETIC PARTICLES

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ONE-DIMENSIONAL ISING MODEL FOR SPIN SYSTEMS OF FINITE SIZE

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QUANTUM ELECTRODYNAMICS OF RESONANCE ENERGY TRANSFER

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