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THE MATCHING METHOD FOR ASYMPTOTIC SOLUTIONS IN CHEMICAL PHYSICS PROBLEMS

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SINGULARLY PERTURBED PROBLEMS WITH BOUNDARY AND INTERIOR LAYERS: THEORY AND APPLICATION*

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NUMERICAL METHODS FOR SINGULARLY PERTURBED BOUNDARY VALUE PROBLEMS MODELING DIFFUSION PROCESSES

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