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THE LIOUVILLE SPACE EXTENSION OF QUANTUM MECHANICS

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* This is a review paper which also contains a number of new results. The reader should compare it with our paper “Poincaré Resonances and the Extension of Classical Mechanics” [1], which will be referred to as “I”.

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UNSTABLE SYSTEMS IN GENERALIZED QUANTUM THEORY

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RESONANCES AND DILATATION ANALYTICITY IN LIOUVILLE SPACE

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QUANTUM SYSTEMS WITH DIAGONAL SINGULARITY

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NONADIABATIC CROSSING OF DECAYING LEVELS

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CAN WE OBSERVE MICROSCOPIC CHAOS IN THE LABORATORY?

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