



# Contents

## Chapter 1. General Introduction

1.1	Introduction . . . . .	1
1.2	Boundary Value Problems and Initial Value Problems . . . . .	4
1.3	One Dimensional Unsteady Flow Characteristics . . . . .	6
1.4	Steady Supersonic Plane or Axi-Symmetric Flow. Equations of Motion in Characteristic Form . . . . .	9
1.5	Basic Concepts Used in Finite Difference Methods . . . . .	15
	References . . . . .	27

## Chapter 2. The Godunov Schemes

2.1	The Origins of Godunov's First Scheme . . . . .	28
2.2	Godunov's First Scheme. One Dimensional Eulerian Equations . . . . .	33
2.3	Godunov's First Scheme in Two and More Dimensions . . . . .	39
2.4	Godunov's Second Scheme . . . . .	41
2.5	The Double Sweep Method . . . . .	46
2.6	Execution of the Second Scheme on the Intermediate Layer . . . . .	48
2.7	Boundary Conditions on the Intermediate Layer . . . . .	50
2.8	Procedure on the Final Layer . . . . .	52
2.9	Applications of the Second Godunov Scheme . . . . .	53
	References . . . . .	56

## Chapter 3. The BVLR Method

3.1	Description of Method for Supersonic Flow . . . . .	57
3.2	Extensions to Mixed Subsonic-Supersonic Flow. The Blunt Body Problem . . . . .	63
3.3	The Double Sweep Method for Unsteady Three-Dimensional Flow . . . . .	67
3.4	Worked Problem. Application to Circular Arc Airfoil . . . . .	69
3.5	Results and Discussion . . . . .	76
	References . . . . .	79

## **Chapter 4. The Method of Characteristics for Three-Dimensional Problems in Gas Dynamics**

4.1	Introduction . . . . .	80
4.2	Bicharacteristics Method (BUTLER) . . . . .	83
4.3	Optimal Characteristics Methods (BRUHN and HAACK, SCHAETZ) . . . . .	90
4.4	Near Characteristics Method (SAUER) . . . . .	95
	References . . . . .	103

## **Chapter 5. The Method of Integral Relations**

5.1	Introduction . . . . .	104
5.2	General Formulation. Model Problem . . . . .	106
5.3	Flow Past Ellipses . . . . .	110
5.4	The Supersonic Blunt Body Problem . . . . .	112
5.5	Transonic Flow . . . . .	116
5.6	Incompressible Laminar Boundary Layer Equations. Basic Formulation . . . . .	121
5.7	The Method in the Compressible Case . . . . .	127
5.8	Laminar Boundary-Layers with Suction or Injection . . . . .	136
5.9	Extension to Separated Flows . . . . .	139
5.10	Application to Supersonic Wakes and Base Flows . . . . .	146
5.11	Application to Three-Dimensional Laminar Boundary Layers	149
5.12	A Modified Form of the Method of Integral Relations . . . . .	160
5.13	Application to Viscous Supersonic Conical Flows . . . . .	164
5.14	Extension to Unsteady Laminar Boundary Layers . . . . . Model Problem (CHU and GONG) . . . . .	168
	References . . . . .	172

## **Chapter 6. Telenin's Method and the Method of Lines**

6.1	Introduction . . . . .	178
6.2	Solution of Laplace's Equation by Telenin's Method . . . . .	179
6.3	Solution of a Model Mixed Type Equation by Telenin's Method	182
6.4	Application of Telenin's Method to the Symmetrical Blunt Body Problem . . . . .	188
6.5	Extension to Unsymmetrical Blunt Body Flows . . . . .	194
6.6	Application of Telenin's Method to the Supersonic Yawed Cone Problem . . . . .	200
6.7	The Method of Lines. General Description . . . . .	212
6.8	Applications of the Method of Lines . . . . .	216
6.9	Powell's Method Applied to Two Point Boundary Value Problems . . . . .	228
	Telenin's Method. Model Problems . . . . .	233
	References . . . . .	247
	<b>Subject Index . . . . .</b>	<b>249</b>

