

ANNALS OF THE NEW YORK ACADEMY OF SCIENCES

VOLUME 316

February 28, 1979

**BIFURCATION THEORY AND APPLICATIONS IN SCIENTIFIC
DISCIPLINES***

Editors and Conference Chairmen

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*This series of papers is the result of a conference entitled Bifurcation Theory and Applications in Scientific Disciplines, held on October 31, November 1, 2, 3, and 4, 1977 and sponsored by The New York Academy of Sciences and the University of Tübingen.

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