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Lectures on Dynamical Systems *

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* Partially supported by N.S.F. Grant MCS 76-05854.

VARIOUS ASPECTS OF INTEGRABLE HAMILTONIAN SYSTEMS (*)

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1. Integrable Hamiltonian Systems

(a) In these informal lecture notes we discuss a number of integrable Hamiltonian systems which have surfaced recently in very different connections. It is our goal to discuss various aspects underlying the integrability of a system like that of group representation, isospectral deformation and geometrical considerations. Since this subject is still far from being understood or being systematic we discuss a number of examples which are seemingly disconnected. In fact, there are some rather unexpected connections

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(*) Partially supported by National Science Foundation Grant MCS 77-01986.