

Computational Aspects of Numerical Models for Weather Prediction and Climate Simulation

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United Kingdom Meteorological Office Five-Level General Circulation Model

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A Description of the NCAR Global Circulation Models

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Computational Design of the Basic Dynamical Processes of the UCLA General Circulation Model

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Global Modeling of Atmospheric Flow by Spectral Methods

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