

Finite Difference Methods for Seismic Wave Propagation in Heterogeneous Materials

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Numerical Analysis of Dispersed Seismic Waves

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Fast Surface Wave and Free Mode Computations

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A Finite Element Method for Seismology

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Seismic Surface Waves

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