

Numerical Solutions of the Integro-Differential Equations of Electron-Atom Collision Theory

P. G. BURKE

DEPARTMENT OF APPLIED MATHEMATICS AND
THEORETICAL PHYSICS
THE QUEEN'S UNIVERSITY, BELFAST, NORTHERN IRELAND

and

M. J. SEATON

DEPARTMENT OF PHYSICS
UNIVERSITY COLLEGE LONDON
LONDON, ENGLAND

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Quantum Scattering Using Piecewise Analytic Solutions

ROY G. GORDON¹

DEPARTMENT OF CHEMISTRY, HARVARD UNIVERSITY,
CAMBRIDGE, MASSACHUSETTS

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Quantum Calculations in Chemically Reactive Systems¹

JOHN C. LIGHT

THE JAMES FRANCK INSTITUTE AND DEPARTMENT OF CHEMISTRY,
THE UNIVERSITY OF CHICAGO, CHICAGO, ILLINOIS 60637

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Expansion Methods for Electron–Atom Scattering¹

FRANK E. HARRIS

DEPARTMENT OF PHYSICS, UNIVERSITY OF UTAH, SALT LAKE CITY, UTAH

and

H. H. MICHELS

UNITED AIRCRAFT RESEARCH LABORATORIES, EAST HARTFORD, CONNECTICUT

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¹ Supported in part at the University of Utah by National Science Foundation Grant GP-11170 and in part at United Aircraft Research Laboratories by the U. S. Air Force Office of Scientific Research under Contract No. AF49(638)-1711.

Calculation of Cross Sections for Rotational Excitation of Diatomic Molecules by Heavy Particle Impact: Solution of the Close-Coupled Equations

WILLIAM A. LESTER, JR.

IBM RESEARCH LABORATORY
SAN JOSE, CALIFORNIA

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Amplitude Densities in Molecular Scattering

DON SECREST

SCHOOL OF CHEMICAL SCIENCE, UNIVERSITY OF ILLINOIS, URBANA, ILLINOIS

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Classical Trajectory Methods

DON L. BUNKER

DEPARTMENT OF CHEMISTRY, UNIVERSITY OF CALIFORNIA AT IRVINE
IRVINE, CALIFORNIA

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