

Energy Bands and the Theory of Solids

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Interpolation Schemes and Model Hamiltonians in Band Theory

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The Pseudopotential Method and the Single-Particle Electronic Excitation Spectra of Crystals

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A Procedure for Calculating Electronic Energy Bands Using Symmetrized Augmented Plane Waves

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Interpolation Scheme for the Band Structure of Transition Metals with Ferromagnetic and Spin-Orbit Interactions*

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Electronic Structure of Tetrahedrally Bonded Semiconductors: Empirically Adjusted OPW Energy Band Calculations*

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The Green's Function Method of Korringa, Kohn, and Rostoker for the Calculation of the Electronic Band Structure of Solids

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