



# Nuclear Optical Model Calculations\*

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# Numerical Methods for the Many-Body Theory of Finite Nuclei

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# Variational Calculations in Few-Body Problems with Monte-Carlo Method

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