

Numerical Simulation of the Earth's Atmosphere¹

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Nonlinear Effects in the Theory of a Wind-Driven Ocean Circulation

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Analytic Continuation Using Numerical Methods

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Numerical Solution of the Complete Krook-Boltzmann Equation for Strong Shock Waves¹

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The Solution of Two Molecular Flow Problems by the Monte Carlo Method

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Computer Experiments for Molecular Dynamics Problems

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Computation of the Stability of the Laminar Compressible Boundary Layer¹

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Some Computational Aspects of Propeller Design

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Methods for the Automatic Computation of Stellar Evolution

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Computations Pertaining to the Problem of Propagation of a Seismic Pulse in a Layered Solid

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