

## Contents

| Preface Acknowledgments |  | ix  |
|-------------------------|--|-----|
|                         |  | xi  |
| Ch                      | apter 1. Probability                                 |     |
| 1.1                     |  | 1   |
| 1.2                     | Conditional Probability and Statistical Independence | 2   |
| 1.3                     |  | 2 3 |
| 1.4                     | Continuous Random Variables                          | 4   |
| 1.5                     | Functions of Random Variables                        | 8   |
| 1.6                     | Characteristic Functions                             | 14  |
| 1.7                     | Averages   | 17  |
|                         | Exercises  | 22  |
|                         | References   | 26  |
|                         | Supplementary Bibliography                           | 26  |
| Cha                     | apter 2. Random Processes                            |     |
| 2.1                     | -  | 27  |
| 2.2                     | Relation to Probability                              | 28  |
| 2.3                     | Ensemble Correlation Functions                       | 30  |
| 2.4                     | Time Averages  | 36  |
| 2.5                     | Time Correlation Functions                           | 39  |
| 2.6                     | Power Spectral Density                               | 39  |
| 2.7                     | Response of Linear Filters                           | 44  |
|                         | Exercises  | 51  |
|                         | References   | 54  |
|                         | Supplementary Bibliography                           | 54  |

vi

| Ch   | apter 3. Narrowband Signals                                   |     |
|------|---|-----|
| 3.1  | Introduction  | 55  |
| 3.2  | Deterministic Signal  | 56  |
| 3.3  | <del>_</del>  | 61  |
| 3.4  |   | 69  |
| 3.5  | Narrowband Filters  | 70  |
| 3.6  | Narrowband Processes  | 75  |
| 3.7  | Fourier Series Representation                                 | 78  |
|      | Exercises   | 83  |
|      | References  | 85  |
|      | Supplementary Bibliography                                    | 85  |
| Cha  | apter 4. Gaussian Derived Processes                           |     |
| 4.1  | Gaussian Properties   | 87  |
| 4.2  | Sum of a Sine Wave and a Gaussian Process                     | 99  |
| 4.3  | Distribution of the Envelope of a Narrowband Gaussian Process | 101 |
| 4.4  | Envelope of a Sine Wave Plus Narrowband Noise                 | 103 |
| 4.5  | Envelope Squared of Narrowband Process                        | 108 |
| 4.6  | Chi-Squared Distribution                                      | 109 |
| 4.7  | Envelope Squared of a Sine Wave Plus a Narrowband Process     | 112 |
| 4.8  | Noncentral Chi-Squared Distribution                           | 113 |
|      | Exercises   | 118 |
|      | References  | 122 |
|      | Supplementary Bibliography                                    | 123 |
| Cha  | apter 5. Hypothesis Testing                                   |     |
| 5.1  | Introduction  | 125 |
| 5.2  | Hypothesis Testing  | 126 |
| 5.3  | Bayes Criterion   | 130 |
| 5.4  | Minimum Error Probability Criterion                           | 132 |
| 5.5  | Neyman-Pearson Criterion                                      | 132 |
| 5.6  | Minimax Criterion   | 135 |
| 5.7  | Multiple Measurements   | 138 |
| 5.8  | Multiple Alternative Hypothesis Testing                       | 140 |
| 5.9  | Composite Hypothesis Testing                                  | 143 |
| 5.10 | Unknown A Priori Information                                  | 146 |
|      | Exercises   | 150 |
|      | References  | 154 |
|      | Supplementary Bibliography                                    | 154 |
| Cha  | apter 6. Detection of Known Signals                           |     |
| 6.1  | Introduction  | 155 |
| 6.2  | A Binary Communication System                                 | 156 |
| 6.3  | The Likelihood Functions                                      | 166 |
| 6.4  | Matched Filters   | 167 |
| 6.5  | An M-ary Communication System                                 | 179 |
| 6.6  | Sampled Approach  | 183 |
|      | Exercises   | 189 |
|      | References  | 193 |
|      | Supplementary Bibliography                                    | 194 |

| CONTENTS | vii |
|----------|-----|
|----------|-----|

| Cha  | apter 7. Detection of Signals with Random Parameters    |     |
|------|---|-----|
|      | Introduction  | 196 |
| 7.2  | Signals with Random Phase                               | 196 |
| 7.3  | The Quadrature Receiver and Equivalent Forms            | 200 |
| 7.4  | Receiver Operating Characteristics                      | 202 |
| 7.5  | Signals with Random Phase and Amplitude                 | 205 |
| 7.6  | Noncoherent Frequency Shift Keying                      | 209 |
| 7.7  | Signals with Random Frequency                           | 216 |
| 7.8  | Signals with Random Time of Arrival                     | 222 |
| 7.9  | Random Frequency and Time of Arrival                    | 224 |
| 7.10 | Sampled Approach  | 225 |
|      | Exercises   | 227 |
|      | References  | 235 |
|      | Supplementary Bibliography                              | 236 |
|      | apter 8. Multiple Pulse Detection of Signals            |     |
|      | Introduction  | 238 |
|      | Known Signals   | 239 |
|      | Signals with Random Parameters                          | 241 |
| 8.4  | Diversity   | 271 |
|      | Exercises   | 276 |
|      | References  | 281 |
|      | Supplementary Bibliography                              | 282 |
| Cha  | apter 9. Detection of Signals in Colored Gaussian Noise |     |
| 9.1  | Introduction  | 285 |
|      | Karhunen-Loeve Expansion                                | 285 |
|      | Detection of Known Signals                              | 290 |
|      | Receiver Performance                                    | 295 |
|      | Optimum Signal Waveform                                 | 297 |
|      | The Likelihood Functions                                | 299 |
|      | Integral Equations                                      | 300 |
| 9.8  | Detection of Signals with Unknown Phase                 | 310 |
|      | Exercises   | 318 |
|      | References  | 319 |
|      | Supplementary Bibliography                              | 316 |
|      | pter 10. Estimation of Signal Parameters                |     |
| 10.1 |   | 321 |
| 10.2 | •   | 322 |
| 10.3 |   | 324 |
| 10.4 |   | 324 |
| 10.5 |   | 325 |
| 10.6 |   | 331 |
| 10.7 | -   | 334 |
| 10.8 |   | 348 |
| 10.9 | Generalized Likelihood Ratio Detection                  | 352 |
|      | Exercises   | 357 |
|      | References  | 360 |
|      | Supplementary Bibliography                              | 361 |

viii

## CONTENTS

| Chaj  | pter 11. Extensions Using Matrix Formulation |     |
|-------|--|-----|
| 11.1  | Introduction                                 | 363 |
| 11.2  | Matrix Preliminaries                         | 364 |
| 11.3  | Multivariate Complex Gaussian Distribution   | 370 |
| 11.4  | Estimation                                   | 371 |
| 11.5  | Best Linear Estimator                        | 372 |
| 11.6  | Maximum Likelihood Estimation                | 374 |
| 11.7  | Maximum A Posteriori Estimation              | 376 |
| 11.8  | Detection                                    | 378 |
| 11.9  | Gaussian Signal in Gaussian Noise            | 380 |
| 11.10 | Space-Time Processing                        | 383 |
|       | Exercises                                    | 395 |
|       | References                                   | 401 |
|       | Supplementary Bibliography                   | 402 |
| INDEX | <b>K</b>                                     | 405 |

