## Contents

| Foreword  |     |
|---|-----|
| Introduction  | 3   |
| Chapter I The Rediscovery of a Mathematical Tool                | 5   |
| I.1 Max Born's Interpretation of Heisenberg's Quantum Condition | 5   |
| I.2 The Development of Matrix Calculus                          | 13  |
| I.3 Early Applications of Matrix Methods in Physics             | 34  |
| I.4 Born's New Collaborator: Pascual Jordan                     | 44  |
| Chapter II Matching the Tools and the Task                      | 61  |
| II.1 The Programme of Matrix Mechanics                          | 62  |
| II.2 Operations with Matrices                                   | 65  |
| II.3 Dynamical Laws and Energy Conservation                     | 72  |
| II.4 An Example of Discrete Mechanics: The Oscillator           | 80  |
| II.5 Preliminary Remarks on Radiation                           | 87  |
| Chapter III Completion of the Matrix Scheme                     | 91  |
| III.1 The Three-Man Collaboration                               | 92  |
| III.2 Towards a New Perturbation Theory                         | 103 |
| III.3 Several Degrees of Freedom and Degeneracy                 | 109 |
| III.4 Born's Idée Fixe and a Letter to Niels Bohr               | 118 |
| III.5 The Eigenvalue Problem and the Transformation to          |     |
| Principal Axes  | 121 |
| III.6 Continuous Spectra and the Significance of the            |     |
| Transformation Matrix   | 129 |
| Chapter IV The Success of Matrix Mechanics                      | 139 |
| IV.1 The Treatment of Dispersion Phenomena                      | 140 |
| IV.2 Fluctuations in Cavity Radiation                           | 149 |
|   |     |

| Contents | ì |
|----------|---|
|----------|---|

| IV.3       | The Conservation of Angular Momentum                           | 157 |
|------------|--|-----|
| IV.4       | Wolfgang Pauli's Conversion                                    | 166 |
| IV.5       | The Solution of the Hydrogen Problem                           | 174 |
| IV.6       | The Problems of Intensities and the Diatomic Molecule          | 185 |
| Chaj       | oter V Modifications and Extensions of Matrix Mechanics        | 195 |
| V.1        | Nonmechanical Stress versus Spin                               | 196 |
| V.2        | Field-Like Representation of Quantum Mechanics                 | 204 |
| V.3        | The Operator Mechanics   | 220 |
| V.4        | Multiply Periodic Systems: Action-Angle Variables and the      |     |
|            | Method of Complex Integration                                  | 247 |
| V.5        | The Electron Spin, Fine Structure and Anomalous Zeeman Effects | 266 |
| V.6        | Key to the Helium Problem                                      | 282 |
| ъс         |  | 202 |
| Keterences |  | 303 |

## Author Index

331