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Note by translators: Our translation of certain Russian words would sometimes have been different from corresponding usages in Radok's English translation of Muskhelishvili's book, "Singular Integral Equations." In such cases, we have conformed to Radok's rendering of the words, since most of our readers will already be familiar with Muskhelishvili's book. In particular, we have consistently made the following two changes:

Canonical → fundamental
 Characteristic → dominant

