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*Additional Results, p. 382*

Where applicable these should be read in conjunction  
with the text

