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# THE RISE OF OXYGEN IN THE EARTH'S ATMOSPHERE WITH NOTES ON THE MARTIAN ATMOSPHERE\*†

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# THE THEORY OF AVAILABLE POTENTIAL ENERGY AND A VARIATIONAL APPROACH TO ATMOSPHERIC ENERGETICS

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