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ATLANTIC AIR-SEA INTERACTION

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THE OPTICAL SPECTRUM OF LIGHTNING

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SCATTERED RADIATION IN THE ATMOSPHERE AND THE NATURAL AEROSOL

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TENSOR CALCULUS IN ATMOSPHERIC MECHANICS

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