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# Resonant scattering of electrons by atomic systems†

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# Type II superconductors

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# The origin of the elements

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# Cosmological models and their observational validation

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# Plasma oscillations

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# Covalent bonding and magnetic properties of transition metal ions

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# Two-beam interferometric spectroscopy

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