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OPTICAL PROPERTIES OF THIN FILMS

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PLANETARY NEBULAE

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PRECISION MEASUREMENT IN GAMMA-RAY SPECTROSCOPY

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^3He INDUCED REACTIONS

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