CONTENTS

A Review of Supersymmetry and Supergravity
J. G. TAYLOR 1

Nearside and Farside: The Optics of Heavy Ion Elastic Scattering
M. S. HUSSEIN and K. W. MCVOY 103

Hyperon–Nucleus Potentials
C. B. DOVER and A. GAL 171

Renormalisation of the Standard Electroweak Model
J. P. COLE 241

Double Beta Decay
W. C. HAXTON and G. J. STEPHENSON, Jr. 409

Author Index 481

Contents of Previous Volumes 489

A REVIEW OF SUPERSYMMETRY AND SUPERGRAVITY

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CONTENTS

1. INTRODUCTION 1
1.1. Preamble 1
1.2. Towards the unification of all forces 2
1.3. The search for a new symmetry 8
2. SUPERSYMMETRIC MODELS 11
2.1. The Wess–Zumino model 11
2.2. Supersymmetric gauge theories 14
2.3. Supersymmetry breaking 15
2.4. Towards a realistic SUSY gauge model 20
*2.5. Extended supersymmetric gauge theories 27
3. SUPERGRAVITY 30
3.1. The construction of supergravity 30
3.2. Extended supergravities 32
3.3. Supergravity in higher dimensions 33
3.4. $N = 8$ supergravity and further symmetries 35
3.5. Spontaneous compactifications 38
3.6. Superunification 40
4. GLOBAL SUPERSPACE 43
4.1. The super-Poincaré algebra 43
4.2. Superfields 47
4.3. The Wess–Zumino model in superspace 52
4.4. Supergraph rules 53
5. GAUGED SUPERSPACE 55
5.1. Supersymmetric gauge theories 55
5.2. $N = 1$ SYM in superspace 56
*5.3. $N = 2$ SYM in superspace 58
5.4. The $N = 3$ barrier in gauged superspace 60
5.5. Quantum properties of supergauge theories 64
*5.6. SYM in light cone superspace 67
6. LOCAL SUPERSPACE 71
6.1. Super-differential geometry 71
6.2. Discovering auxiliary fields 74
6.3. Constrained superspace 79
6.4. Superspace supergravity actions 85
6.5. Supergravity ultra-violet divergences 86
6.6. The $N = 3$ barrier in local superspace 88
*6.7. Central charges 91
7. CONCLUSIONS AND FUTURE DIRECTIONS 95
ACKNOWLEDGEMENTS 96
REFERENCES 96

1. INTRODUCTION

1.1. Preamble

Supersymmetry is a proposed symmetry of nature in
indistinguishable. In the form it is known and used today it was first introduced by Wess

CONTENTS

1. INTRODUCTION 104
   1.1. Purpose of the review 104
   1.2. The 2-slit pattern for absorbers: Edge waves 105
   1.3. Examples of Near-side/Far-side decompositions 108
   1.4. Geometry-dominance in Born approximation 111
   1.5. Further examples 114
2. ELEMENTARY SEMI-CLASSICAL TECHNIQUES AND IMPORTANT OPTICAL THEOREMS 117
   2.1. The Stationary-phase or saddle-point approximation to oscillatory integrals 118
   2.2. The Near/Far decomposition 119
      2.2.1. *Physical ideas and approximate formulae* 119

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2.2.2. *Essential properties:* 121
2.2.2.1. "Exploring the potential" 121
2.2.2.2. Single-trajectory dominance of σ_N and σ_F 122
2.2.2.3. Running waves in angle 122
2.2.2.4. Real phase shifts and rainbow shadows 122
2.2.2.5. Absorption and diffractive shadows 124
2.2.3. The correct mathematics, à la Fuller 124
3. A Few Essential Properties of Heavy-ion Angular Distributions 125
3.1. Exponential shadow tails from peripheral ℓ-windows 125
3.2. Babinet symmetry for pure absorbers 126
3.3. The single-slit edge wave of an absorber 127
3.4. Slopes of exponential shadows: orbiting at complex ℓ 128
3.5. External refractors: The Coulomb prism 132
4. Practical Applications and Examples 134
4.1. Summary of Sections 2 and 3 134
4.2. The influence of nuclear refraction: $^9Be + ^{16}O$ at 158 MeV 135
4.3. Nuclear rainbows? 138
4.4. A hidden rainbow 144
4.5. The case of the transparent surface 144
4.6. Potential ambiguities 148
4.7. Just for fun 153
4.7.1. *Another hidden rainbow?* 153
4.7.2. *A bizarre α-dip* 153
4.7.3. *A pure Coulomb rainbow* 154
4.7.4. *Pure glass* 155
5. Nuclear Forward-glory Scattering 155
6. Deviations from Optical Behavior 158
6.1. Anomalous back-angle scattering 158
6.2. Static and dynamic deformation effects: Long range absorption 160
7. Summary 163
Acknowledgements 165
References 165
Notes Added in Proof 166
Appendix A. The Deflection Function and Fermat: Lenses as Phase-Shifters 167
Appendix B. The Knoll–Schaeffer–Glauber–Born Approximation to the Deflection Function in the $E \gg V$ limit 169

CONTENTS

1. Introduction 172
2. One Boson Exchange Models for the Two Body Problem 174
3. The Effective Two-Body Interaction 197
4. Single Particle Potentials for Baryons in the Nucleus 202
5. Selected Numerical Results 211
6. Hypernuclear Widths 221
7. Conclusions 234
Acknowledgements 237
References 237

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CONTENTS

NOTATION, SYMBOLS AND ABBREVIATIONS 242
INTRODUCTION 243
1. INTRODUCTION TO GAUGE THEORIES 245
1.1. Symmetries in field theories 245
1.2. Gauge fields 247
1.3. Yang–Mills field 248
1.4. Spontaneously broken symmetry 249
2. QUANTISATION OF FIELD THEORIES AND THE STANDARD ELECTROWEAK MODEL 252
2.1. Quantisation of scalar field theory 252
2.2. Quantisation of gauge theories 257
2.3. The standard electroweak model 261
3. RENORMALISATION OF THE MODEL 272
3.1. Renormalisation of ϕ^4 theory 272
3.2. Renormalisation of the vector boson propagator 276
3.3. Renormalisation of the fermion propagator 278
3.4. Example calculations in QED 279
3.5. Other schemes of renormalisation 283
3.6. Renormalisation of the GWS model (Part 1) 285
3.7. Renormalisation of the GWS model (Part 2) 292
4. GAUGE INVARIANCE AND RENORMALISATION 296
4.1. The fermion self-energies 297
4.2. The fermion charges 301
4.3. The fermion–Z coupling 305
4.4. Gauge-invariance of the neutral current scattering amplitudes 307
4.5. Gauge-invariance of the charged scattering amplitudes 315
4.6. Search for a fourth condition 320
5. CALCULATION OF THE RENORMALISATION CONSTANTS 328
5.1. The fermion self-energies 328
5.2. General three-point functions 329
5.3. The fermion charges 331
5.4. The boson renormalisation constants 333
6. ONE LOOP DIAGRAMS 338
6.1. Weak corrections to the neutral currents 338
6.1.1. *Vertex corrections* 338
6.1.2. *Bosonic corrections* 340
6.1.3. *The box diagrams* 342
6.2. Weak corrections to the charged currents 344
6.2.1. *Vertex corrections* 344
6.2.2. *The box diagrams* 346
6.2.3. *The W-boson self-energy* 348
6.3. Photononic corrections 348
6.3.1. *Box diagrams* 349
6.3.2. *Vertex corrections* 349
6.3.3. *The Bremßtrahlung cross-sections* 351
6.3.4. *The finite results* 351

7. Experimental Corrections 353
7.1. Neutrino experiments 353
7.2. The corrections to the Fermi coupling constant, G_F 361
7.3. Polarised electron scattering experiments 365
7.4. Conclusions 371
Appendix 1. The Solution of Tensor Equations[56] 372
Appendix 2. The Dimensional Regularisation Method 373
A.2.1. Feynman parametrisation 373
A.2.2. Formulae of dimensional regularisation 375
Appendix 3. Gamma Matrix Algebra 379
A.3.1. Trace identities 380
A.3.2. Matrix identities 380
A.3.3. ε-tensor identities 381
A.3.4. Matrices between Dirac spinors 381
A.3.5. V, A matrices 382
Appendix 4. Tadpole Contributions to Boson Self-energies 383
Appendix 5. Calculation of Parameter Integrals 385
Appendix 6. Numerical Analysis of the Results 395
A.6.1. Boson self-energies 397
A.6.2. Weak corrections to the ν-scattering cross-sections 397
A.6.3. Photonic corrections to the ν-scattering cross-sections 398
A.6.4. Weak corrections to e–D scattering asymmetry 403
Appendix 7. A Note on the Minimal Subtraction Scheme 403
A.7.1. QED 405
A.7.2. GWS model 406
References 407

DOUBLE BETA DECAY*

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CONTENTS

1. INTRODUCTION 410
2. EXPERIMENTAL EVIDENCE 413
   2.1. Occurrence of $\beta\beta$ decay 413
   2.2. Direct detection experiments 417
   2.3. Geochemical half life determinations 421
   2.4. Radiochemical experiments 425
3. THEORETICAL TREATMENT 425
   3.1. The Hamiltonian 425
   3.2. The neutrino mass matrix and CP properties 427
   3.3. Derivation of two-nucleon 2ν and 0ν $\beta\beta$ decay rates 430
      3.3.1. *Two-nucleon mechanism for* 2ν $0^+ \to 0^+$ *decay in the standard model* 430
      3.3.2. *Two-neutrino* $0^+ \to 1^+$ *and* $0^+ \to 2^+$ *decays* 435
      3.3.3. *Two-nucleon mechanism for* 0ν $0^+ \to 0^+$ *decays* 436
      3.3.4. *Neutrinoless* $0^+ \to 1^+$ *and* $0^+ \to 2^+$ *decays* 440
   3.4. The neutrino propagator for light and heavy neutrinos 443
      3.4.1. *First approximation: Light or heavy neutrinos* 443
      3.4.2. *Light neutrinos* 444
      3.4.3. *Effects due to finite nuclear size* 444
      3.4.4. *Correlations* 445
   3.5. The neutrino mass in $\beta\beta$ and constraints imposed by CP conservation 445
      3.5.1. *Dirac limit* 446
      3.5.2. *Majorana limit* 447
      3.5.3. *Dominant right-handed mass limit* 447
      3.5.4. *Pseudo-Dirac limit* 447
   3.6. Transitions involving nucleon isobars 448
   3.7. Mechanisms beyond the standard model 450
   3.8. Positron-emitting electron capture and double electron capture 451
4. NUCLEAR STRUCTURE 452
   4.1. General observations 452
   4.2. Nuclear calculations 453
   4.3. Other structure studies 455
   4.4. Theoretical approximations: Are there any surprises? 458
5. RATES FOR $\beta\beta$ DECAY AND LIMITS ON LEPTON NUMBER VIOLATION 459
   5.1. $0^+ \to 0^+$ and $0^+ \to 2^+$ 2ν decay rates 459
   5.2. $0^+ \to 0^+$ 0ν decay and light-mass neutrinos 460
   5.3. $0^+ \to 0^+$ 0ν decay mediated by heavy neutrinos 469
   5.4. $0^+ \to 2^+$ 0ν decay 471
6. SUMMARY AND CONCLUSIONS 472
APPENDIX: COULOMB CORRECTIONS AND PHASE-SPACE ESTIMATES OF 2ν HALF LIVES 473
REFERENCES 475

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