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THE COMPOSITION OF THE PRIMARY COSMIC RADIATION

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COLLECTIVE MOTION IN NUCLEI

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DISPERSION RELATIONS FOR ELEMENTA PARTICLES

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CHERENKOV DETECTORS

G. W. HUTCHINSON

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THE PHOTOPRODUCTION OF PIONS

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