

Contents

The Master Equation Approach: Coherence, Energy Transfer, Annihilation, and Relaxation

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1.	<i>Background</i>	1
1.1	Introduction	1
1.2	The System and the Questions	1
2.	<i>Coherence and the Generalized Master Equation Approach: Formalism</i>	3
2.1	Introduction	3
2.2	Motivation for the GME Approach	5
2.3	General Derivation of Exciton GME's	7
2.4	Range of Validity of Exciton GME's	10
2.5	A Conceptual Application: Unification of Transfer Rates	13
2.6	Evaluation of Memory Functions	16
2.6.1	Pure Crystal of Arbitrary Size: Nonlocal Memories	16
2.6.2	Crystal in Interaction with a Bath: Long-Range Transition Rates	19
2.6.3	Linear Exciton-Phonon Coupling	23
2.6.4	Generalization of Förster's Spectral Prescription	27
2.6.5	Present Status of Available Memories	32
2.7	Relation of GME's to Other Transport Entities	33
2.7.1	Relation of GME to the Pauli Master Equation	33
2.7.2	Relation of GME to the Stochastic Liouville Equation	34
2.7.3	Relation of GME to Continuous-Time Random Walks	38
2.7.4	Relation of GME to Velocity Autocorrelation Functions	39
2.7.5	Relation of GME to the Scattering Function	42
3.	<i>Coherence and the Generalized Master Equation Approach: Application to Experiments</i>	43
3.1	Introduction	43
3.2	Transient Grating Observations	43
3.2.1	A Universal Connection	44
3.2.2	Nonexponential Signals and Coherence	46

3.2.3	Exponential Signals and Coherence	48
3.2.4	Further Calculations	49
3.3	Sensitized Luminescence	50
3.3.1	Formulation: the Simplest Trapping Model	51
3.3.2	Unified Description of the Effect of Coherence on Yields	54
3.3.3	More General Trapping Models	58
3.3.4	Further Calculations	62
3.4	Annihilation Observations	64
3.4.1	Technique of Solution	65
3.4.2	Expressions for Observable Quantities	68
3.4.3	Validity of the Bilinear Equation and Expressions for γ	71
3.4.4	Further Calculations	74
4.	<i>Other Issues and Other Master Equation Techniques</i>	75
4.1	Introduction	75
4.2	Master Equations for Surface Quenching	75
4.2.1	Effect of Imperfect Absorption by End Detectors	76
4.2.2	Effect of Variation in Penetration Length	81
4.2.3	Further Developments in Surface Quenching	82
4.3	Master Equation Analysis of the Energy Transfer Rate	84
4.3.1	Time-Dependent Energy Transfer Rates	85
4.3.2	Steady-State Energy Transfer Rates	87
4.4	Momentum-Space Master Equations for Trapping	89
4.4.1	k -Space Equations and Trapping Rates	89
4.4.2	Expressions for Luminescence Observables	91
4.5	Master Equations for the Interplay of Vibrational Relaxation with Exciton Motion	93
4.5.1	Formalism and Technique of Solution	93
4.5.2	Explicit Expressions and Time-Dependent Transition Rates for Exciton Motion	96
5.	<i>Conclusion</i>	99
5.1	Summary of the Master Equation Approach	99
5.2	Future Work	102
	<i>References</i>	104

**Stochastic Liouville Equation Approach:
Coupled Coherent and Incoherent Motion, Optical Line Shapes,
Magnetic Resonance Phenomena**

By P. Reineker. With 28 Figures

1. <i>Introduction</i>	111
2. <i>Model of the Coupled Coherent and Incoherent Exciton Motion and its Stochastic Liouville Equation</i>	117
2.1 The Coherent Motion of the Excitons	117
2.2 The Incoherent Motion of the Excitons	120
2.3 The Stochastic Liouville Equation for the Exciton Density Operator .	121
3. <i>Coupled Coherent and Incoherent Exciton Motion in Molecular Pairs and on a Linear Chain</i>	125
3.1 Exciton Motion in Molecule Pairs	125
3.2 Exciton Motion on a Linear Chain of Molecules	129
3.2.1 The Equation of Motion	129
3.2.2 Solution of the Eigenvalue Equation	130
3.2.3 Time Development of an Initially Localized Excitation	134
4. <i>Mean-Square Displacement and Diffusion Equation of Excitons</i>	135
4.1 Moments of the Exciton Motion	136
4.2 Derivation of a Diffusion Equation	139
4.2.1 Master Equation for the Exciton Motion	139
4.2.2 Diffusion Equation for the Exciton Motion	141
5. <i>Optical Absorption of Molecular Crystals with Two Differently Oriented Molecules in the Unit Cell</i>	142
5.1 Two-Time Correlation Functions	142
5.2 Equations of Motion for Correlation Functions	143
5.3 Optical Line Shape of Anthracene Type Molecular Crystals	144
5.4 Extensions to Non-Markovian Fluctuations	148
6. <i>Electron-Spin Resonance in Molecular Crystals with Two Differently Oriented Molecules in the Unit Cell</i>	149
6.1 ESR Line Shape of Excitons with Spin 1/2 in Dimers of Inequivalent Molecules	150
6.1.1 Effective Hamiltonian and Equations of Motion for Correlation Functions	150
6.1.2 Calculation of the ESR Line Shape	152
6.1.3 ESR Line Shape in the Completely Incoherent Case	154
6.1.4 ESR Line Shape for the Coupled Coherent and Incoherent Exciton Motion	155

6.1.5 Approximate Expressions for the Line Shapes	157
a) Expansion at $\omega = A + B$ for $\gamma_0 < 2J$ (Coherent Exciton Motion)	158
b) Expansion at $\omega = A + B$ for $\gamma_0 \gg J$ (Incoherent Exciton Motion) and $2\gamma_1, J^2/\gamma_0 \gg A - B $	158
c) Expansion at $\omega = A + B$ for very large γ_0 (Limiting Case of the Hopping Model for the Exciton Motion)	159
d) Expansion at $\omega = 2A$ for $\gamma_0 \gg 2J$ (Incoherent Exciton Motion) and $2\gamma_1, J^2/\gamma_0 \ll A - B $	159
6.2 ESR Line Shape of Triplet Excitons in Dimers of Inequivalent Molecules (AB Pairs)	160
6.2.1 The Parameters of the Model	161
6.2.2 ESR Line Positions in the Completely Coherent Case	162
6.2.3 ESR Line Shape for the Coupled Coherent and Incoherent Exciton Motion	164
a) Calculation of the Line Shape	164
b) Results and Discussion	165
6.3 ESR of Quasi-Incoherent Excitons in Molecular Crystals with Two Differently Oriented Molecules in the Unit Cell	170
6.3.1 Equation of Motion for Correlation Functions in the Quasi-Incoherent Case of Exciton Motion	171
6.3.2 Exact Calculation of the ESR Line Shape of Quasi-Incoherent Triplet Excitons in Molecular Crystals with Two Molecules in the Unit Cell	177
6.3.3 Eigenvalues Describing the ESR Line Shape	181
6.3.4 Analytical Calculation of the Eigenvalues Determining the ESR Line in the Case of Rapid Exciton Motion	186
a) Rotation of the Magnetic Field Around the a and c' Axes ..	187
b) Rotation of the Magnetic Field Around the b Axis	188
6.3.5 Comparison with Experimental Data	189
a) Line Positions	189
b) Line Widths	190
6.4 Investigation of the Coherent One-Dimensional Motion of Triplet Excitons by Spin Resonance	193
7. Influence of the Exciton Motion on Proton Relaxation in Organic Solids ..	194
7.1 Bloch Equations for the Proton Spins	194
7.2 Calculation of the Spectral Density	197
7.2.1 Coupled Coherent and Incoherent Motion of Excitons in a Dimer	197
7.2.2 Purely Coherent Exciton Motion on a Linear Chain	198
7.2.3 Purely Incoherent Exciton Motion on a Linear Chain	199
8. Connection Between Stochastic Liouville Equation and Generalized Master Equation Treatments	200

8.1 Stochastic Liouville and Nakajima-Zwanzig Equations	200
8.2 Calculation of the Kernel K(t)	201
8.2.1 Definition of the Projection Operator	201
8.2.2 Transformation of the Kernel	202
8.2.3 Calculation of Matrix Elements	203
8.3 Generalized Master Equation for the Coupled Coherent and Incoherent Motion of Excitons	205
8.4 Investigation of Limiting Cases	208
8.4.1 Purely Incoherent Exciton Motion	208
8.4.2 Purely Coherent Exciton Motion	209
8.4.3 Quasi-Incoherent Exciton Motion	209
8.4.4 The Case $\bar{\gamma} = 0$	210
8.4.5 Derivation of the Generalized Master Equation in the Born Approximation	210
<i>Appendix A.</i> Equation of Motion for the Density Operator	212
<i>Appendix B.</i> Green's Function of the Exciton Motion on a Linear Chain	215
<i>Appendix C.</i> Angular Dependence of ESR Line Position and Width	216
C.1 Rotation Around the a Axis	217
C.2 Rotation Around the b Axis	218
C.3 Rotation Around the c' Axis	219
<i>References</i>	220