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# Paramagnetische Felder am Kernort

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# Group Theory and Spectroscopy\*

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# Continuous Groups in Quantum Mechanics<sup>\*,\*\*</sup>

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# Determination of Nuclear Moments with Optical Double Resonance

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# Rigorous Symmetries of Elementary Particles\*

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