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# HOLOGRAPHY AND DOUBLE PHASE CONJUGATION

H. JAGANNATH AND H. J. CAULFIELD

*Department of Physics, Alabama A & M University,  
Normal, AL*

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# LASER AND PULSED-LASER NMR SPECTROSCOPY

M. W. EVANS\*

*Cornell Theory Center, Cornell University, Ithaca, NY  
and  
Materials Research Laboratory, The Pennsylvania State University,  
University Park, PA*

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\*Present address: Department of Physics, University of North Carolina, Charlotte, NC 28223.

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# SOME PROPERTIES OF LONGITUDINAL FIELDS AND PHOTONS

M. W. EVANS\*

*Department of Physics, University of North Carolina,  
Charlotte, NC*

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\*Senior Visiting Research Associate, Materials Research Laboratory, Pennsylvania State University, University Park, PA 16802-4801; Visiting Scientist and Leverhulme Fellow, Cornell Theory Center, Ithaca, NY 14853.

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***THE MAGNETOSTATIC FLUX DENSITY  $B_{\Pi}$  OF  
THE ELECTROMAGNETIC FIELD:  
DEVELOPMENT AND CLASSICAL  
INTERPRETATION***







# **FREQUENCY-DEPENDENT CONTINUUM ELECTROMAGNETIC PROPERTIES OF A GAS OF SCATTERING CENTERS**

**AKHLESH LAKHTAKIA**

*Department of Engineering Science and Mechanics, The Pennsylvania  
State University, University Park, PA*

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# **ASPECTS OF THE OPTICAL KERR EFFECT AND COTTON-MOUTON EFFECT OF SOLUTIONS**

**JEFFREY HUW WILLIAMS**

*Institut Max von Laue-Paul Langevin, Grenoble, France*

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**AHMED A. HASANEIN**

*Department of Chemistry, College of Sciences, King Sand University,  
Riyadh, Saudi Arabia, and Department of Chemistry, Faculty  
of Science, Alexandria University, Alexandria, Egypt*

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G. E. STEDMAN

*Department of Physics, University of Canterbury,  
Christchurch 1, New Zealand*

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DAVID L. ANDREWS

*School of Chemical Sciences, University of East Anglia,  
Norwich, England*

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A. S. PARKINS

*Joint Institute for Laboratory Astrophysics, and Department of  
Physics, University of Colorado, Boulder, Colorado*

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# THE EFFECTIVE EIGENVALUE METHOD AND ITS APPLICATION TO STOCHASTIC PROBLEMS IN CONJUNCTION WITH THE NONLINEAR LANGEVIN EQUATION

W. T. COFFEY

*School of Engineering  
Department of Microelectronics & Electrical Engineering  
Trinity College Dublin, Ireland*

YU. P. KALMYKOV

*Institute of Radio Engineering and Electronics  
Russian Academy of Sciences  
Fryazino, Moscow Region, Russia*

E. S. MASSAWE

*School of Engineering  
Department of Microelectronics & Electrical Engineering  
Trinity College Dublin, Ireland*

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