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THE COLLISIONAL TIME-CORRELATION FUNCTION APPROACH TO MOLECULAR ENERGY TRANSFER

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MOLECULAR THEORY OF LIQUID-PHASE VIBRATIONAL ENERGY RELAXATION

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ONE-DIMENSIONAL QUANTUM MECHANICAL PROBLEMS WITH COMPLICATED POTENTIALS. THE PROPAGATOR METHOD OF SOLUTION AND SOME CHEMICAL APPLICATIONS

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