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# INTERNAL EXCITATIONS IN LIQUIDS

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# **EQUILIBRIUM AND DYNAMICAL FOURIER PATH INTEGRAL METHODS**

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# **FLUCTUATING NONLINEAR HYDRODYNAMICS, DENSE FLUIDS, AND THE GLASS TRANSITION**

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# **STRUCTURE OF THE ELECTRIC DOUBLE LAYER**

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# **DYNAMICS OF DENSE POLYMER SYSTEMS: COMPUTER SIMULATIONS AND ANALYTIC THEORIES**

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