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MATRIX-FORMULATED DIRECT MULTICONFIGURATION SELF-CONSISTENT FIELD AND MULTICONFIGURATION REFERENCE CONFIGURATION- INTERACTION METHODS

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THE MULTICONFIGURATION SELF- CONSISTENT FIELD METHOD

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PROPAGATOR METHODS

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ANALYTICAL DERIVATIVE METHODS IN QUANTUM CHEMISTRY

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SYMMETRY AND DEGENERACY IN $X\alpha$ AND DENSITY FUNCTIONAL THEORY

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MODERN VALENCE BOND THEORY

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**אָבּוֹן מְאָסֵן הַבּוֹנִים
חַיְתָה לְרֹאשׁ פָּנָה**

The stone rejected by the builders
Is become the chief cornerstone

THE COMPLETE ACTIVE SPACE SELF- CONSISTENT FIELD METHOD AND ITS APPLICATIONS IN ELECTRONIC STRUCTURE CALCULATIONS

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TRANSITION-METAL ATOMS AND DIMERS

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WEAKLY BONDED SYSTEMS

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