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# EXCITED-STATE POTENTIALS

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# MOLECULAR PROPERTY DERIVATIVES

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# TRANSITION STRUCTURE COMPUTATIONS AND THEIR ANALYSIS

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# OPTIMIZATION OF EQUILIBRIUM GEOMETRIES AND TRANSITION STRUCTURES

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# RELATIVISTIC QUANTUM CHEMISTRY

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# EFFECTIVE HAMILTONIANS AND PSEUDO-OPERATORS AS TOOLS FOR RIGOROUS MODELLING

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# MOLECULAR CALCULATIONS WITH THE DENSITY FUNCTIONAL FORMALISM

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# BASIS SETS

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# THE COUPLED PAIR APPROXIMATION

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