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TAGGED-PARTICLE MOTION IN DENSE MEDIA: DYNAMICS BEYOND THE BOLTZMANN EQUATION

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ON INVARIANCE OF LOCALIZED HAMILTONIANS UNDER FEASIBLE ELEMENTS OF THE NUCLEAR PERMUTATION-INVERSION GROUP

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COLLISIONAL DISSOCIATION AND CHEMICAL RELAXATION OF RUBIDIUM AND CESIUM HALIDE MOLECULES

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THE VIRIAL THEOREM

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[‡]Based on the Dissertation of Guilhem Marc for the degree of Doctor of Philosophy in Chemistry, University of California, Los Angeles, 1983.

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