

CONTENTS

FUNCTIONAL INTEGRALS AND POLYMER STATISTICS <i>By Karl F. Freed</i>	1
EQUILIBRIUM DENATURATION OF NATURAL AND OF PERIODIC SYNTHETIC DNA MOLECULES <i>By Roger M. Wartell and Elliott W. Montroll</i>	129
THE LATTICE VIBRATIONS OF MOLECULAR SOLIDS <i>By O. Schnepp and N. Jacobi</i>	205
AN INTRODUCTION TO C*-ALGEBRAIC METHODS IN PHYSICS <i>By Gérard G. Emch</i>	315
RADIATIVE AND NONRADIATIVE PROCESSES IN BENZENE <i>By C. S. Parmenter</i>	365
AUTHOR INDEX	423
SUBJECT INDEX	433



FUNCTIONAL INTEGRALS AND POLYMER STATISTICS

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CONTENTS

I. Introduction	2
II. Brief Summary of the Configurational Statistics of Polymer Chains	7
A. Background	7
B. Flexible and Stiff Polymer Chains	10
C. Review of Configurational Statistics of Flexible Polymer Chains	11
D. The Wormlike Chain	21
III. Introduction to Functional Integration: Flexible Polymer Chains	23
A. The Wiener Integral	23
B. The Relation to Diffusion and Brownian Motion	25
IV. Feynman Path Integrals in Quantum Mechanics	32
V. Introduction to Functional Integration: Stiff Polymer Chains	35
A. Introduction.	35
B. Stiffness	37
C. An Analogy with Brownian Motion.	38
D. The Reduced Distributions	39
E. The STY Approach	41
F. The Simpler Model	43
G. Generalized Models	48
H. Discussion	53
Appendix A. Direct Evaluation of the "Harmonic Oscillator" Green's Function (5.15)	54
VI. The Excluded Volume Problem: The Self-Consistent Field	59
A. The Long-Range Interactions	61
B. Survey of the Different Approaches to the Problem	63
C. Introduction of the SCF	65
D. Formal Derivation of the SCF Equations.	69
E. Comparison with Diagrammatic Approaches to the Excluded Volume Problem	74
F. Approximate SCF Solution	76
G. Nonideal Polymer Solutions	79

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Appendix B: The Hierarchy	80
Appendix C: The Saddle Points ϕ_0 and ϕ_1	82
VII. Polymers in Bulk: Introduction	84
VIII. Is There a Polymer Analog of the Perfect Gas?	86
IX. Statistical Mechanics with Constraints: Introduction	94
A. The Constraints	95
B. Small Changes of State	98
C. The Polymer in a Box with Constraints	101
D. General Changes of State	105
X. Polymers in Bulk: A Field Theory	107
References	126

EQUILIBRIUM DENATURATION OF NATURAL AND OF PERIODIC SYNTHETIC DNA MOLECULES

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TABLE OF CONTENTS

I. Introduction	130
A. General Background	130
B. Theoretical Models	131
C. Naturally Occurring DNA Molecules	132
D. Synthetic DNA Molecules	135
II. Modified Ising Model	138
A. Periodic DNAs without Branching	145
B. Periodic DNAs with Branching	149
C. Unbranched Periodic DNAs with Strand Sliding	153
D. DNAs with a Random Distribution of Two Bond Types	155
1. Theory of Montroll and Yu	155
2. Lehman-McTague Theory	164
3. Vedenov-Dyhkne Theory	167
III. Loop Entropy Model	169
A. Periodic DNAs without Branching	169
1. One-Component DNA	170
2. Two-Component DNA	174
B. Periodic DNAs with Branching	178
C. DNAs with a Random Distribution of A-T and G-C Pairs	179
IV. Comparison of Theories with Experiment	186
A. Periodic DNAs	186
B. Natural DNAs	191
V. Discussion	194
References	196
Appendix A End Effects for Long DNA Chains	198
Appendix B Four-Component Specific Sequence Algorithms	200
Appendix C Experimental Materials and Procedures	201

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THE LATTICE VIBRATIONS OF MOLECULAR SOLIDS*

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CONTENTS

I. Introduction	206
II. Classical Lattice Dynamics	208
A. The Intermolecular Potential Model	208
B. Treatment of Translational Motions	210
1. General	210
2. Classical Treatment	210
3. Lattice Dynamics in Terms of Translationally Symmetric Coordinates	212
4. The Hamiltonian of the Lattice Dynamics Problem	215
5. Molecular Solids	216
C. Treatments Including Librational Motions	217
1. General	217
2. Libration as Harmonic Oscillator	217
3. Cartesian Coordinate Treatment	222
4. Matrix Treatment	223
5. Direction Cosine Displacement Coordinates	226
6. Infinitesimal Rotation Coordinates	231
7. Eulerian Angle Displacement Coordinates	233
8. Extended Point-Mass Model.	236
D. Translation-Libration Interactions and Solution of the Lattice Dynamics Problem	237
E. Symmetry Relations between Force Constants	238
F. Applications and Comparison with Experiment	244
1. Inorganic Molecular Solids	244
2. Organic Molecular Solids	255
III. Quantum Lattice Dynamics	263
A. General Remarks	263
B. Single-Particle Model	264
C. Three-Dimensional Case	265
D. Correlation Corrections	268
1. Introduction	268
2. Long-Range Correlation	268
3. Short-Range Correlation	270

* This work was supported by a grant from the National Science Foundation and from the the Army Research Office-Durham.

E. Temperature Dependence	272
F. Applications and Comparison with Experiment	272
1. Solid Helium	272
2. Other Rare Gas Solids	274
3. Solid Hydrogen	275
IV. Intensities of Lattice Vibration Spectra	276
A. Introduction	276
B. Infrared Intensities	277
1. General	277
2. Intrinsic Transition Moment—Librations of Polar Molecules	279
3. Induced Transition Moment—Translational Modes	281
C. Raman Intensities	285
D. Applications and Comparison with Experiment	286
1. α -Nitrogen	286
2. Carbon Dioxide	289
3. Nitrogen Dioxide	290
4. Solid Hydrogen	290
5. Cyanogen	291
6. Halogen Solids	291
7. Carbon Monoxide	291
8. ClCN and BrCN	292
9. HCl and HBr	292
10. OCS	292
E. Discussion of Results	292
Appendix. Group Theory and Symmetry in the Brillouin Zone as Applied to Lattice Dynamics of Molecular Solids	293
I. Introduction	293
II. Transformation of the Basis Functions	295
III. Determination of Symmetry Species of Lattice Vibrations and Applications to Solid Naphthalene	299
IV. Application to Solid CO ₂	303
References	309

AN INTRODUCTION TO C^* -ALGEBRAIC METHODS IN PHYSICS†

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CONTENTS

Part I. General Motivation	317
I. Quantum Field Theory and Statistical Mechanics: Two Facets of the Same Problem	317
A. Generalities	317
B. The Usual Formalism of Quantum Mechanics	317
C. BCS Model	319
D. van Hove Model	321
E. Summary	323
F. The C^* -Algebraic Approach	323
G. Historical Background	325
H. Bibliography	326
Part II. Tools and Techniques	327
II. Representation Theory: The Richness of the C^* -Algebraic Approach	327
A. Generalities	327
B. The GNS Construction	327
C. Irreducible Representations	330
D. Application to the Canonical Commutation Relations	331
E. von Neumann Theorem	332
F. Fock Space	333
G. The Free Bose Gas	334
H. Bibliography	335
III. Symmetries, Cluster Properties, and the KMS Condition	335
A. Generalities	335
B. Covariant Representations	337
C. Averages	337

† This chapter is based on a series of six lectures given at the Service de Chimie Physique II, Université Libre de Bruxelles, January–February 1971, under the auspices of the Solvay Seminars. The choice of the material presented reflects merely the particular bias of the lecturer, tempered by the interests of the audience.

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D. Extremal G -Invariant States, η -Clustering, and Ergodicity	339
1. Preliminary Remarks	339
2. The Principal Theorem	339
E. Formulation of the KMS Condition	340
F. Elementary Consequences of the KMS Condition	341
G. Bibliography	343
Part III. Applications	344
IV. Spin Systems and Lattice Gases	344
A. Generalities	344
B. The Quasi-Local Algebra of a Spin System	344
C. Time-Evolution	346
D. Some Variations on the Theme of the Transfer Matrix Formalism	346
E. Generalizations to Classical Systems	347
F. General Heisenberg Models in One Dimension	349
G. Weiss Model for Antiferromagnetism	351
H. Bibliography	352
V. Crystallization as a Symmetry-Breaking Process	353
A. Generalities	353
B. Decomposition Theory	354
C. Restrictions Imposed on the Theory	355
D. Fluid Phase	356
E. Nonfluid Phases	357
F. Concluding Remarks	358
G. Bibliography	358
VI. Nonequilibrium and Ergodicity	358
A. Generalities	358
B. Description of One Experiment	359
C. Elementary Theoretical Analysis	360
D. Elementary Exploitation of this Analysis	360
E. Algebraic Formulation	361
F. Noncommutative Ergodic Theory	362
G. Bibliography	364
Acknowledgments	364

RADIATIVE AND NONRADIATIVE PROCESSES IN BENZENE*

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CONTENTS

I. Introduction	365
II. The $\pi\pi^*$ Excited States	368
A. The Singlet States	369
B. The Triplet States	372
C. Vibrational Frequencies	374
III. ${}^1B_{2u} - {}^1A_{1g}$ Spectroscopy	376
A. Single Vibronic Level Fluorescence	377
B. Franck-Condon Factors in SVL Fluorescence	384
C. SVL Fluorescence and the ${}^1B_{2u} - {}^1A_{1g}$ Absorption Spectrum	385
IV. Relaxation of the ${}^1B_{2u}$ State in the Vapor—General Considerations	389
V. Relaxation from the Thermal Vibrational Levels	392
A. Partitioning of Radiative and Nonradiative Decay	395
B. Identification of the Nonradiative Channel	397
C. Photochemistry from the Thermal Vibrational Levels	402
VI. Relaxation from the “Higher” Vibrational Levels	403
VII. Relaxation from Isolated ${}^1B_{2u}$ Molecules at Low Pressures	407
A. Relaxation from Levels Excited with the 2536 Å Hg Line	408
B. Relaxation from Single Vibronic Levels	411
Acknowledgments	418
References	418