

CONTENTS

Toward an Analytic Theory of Chemical Reactions	
<i>By Henry Aroeste</i>	1
<i>Manuscript received April, 1962</i>	
Electron Gas in a Lattice of Positive Charges	
<i>By A. Bellemans and M. de Leener</i>	85
<i>Manuscript received April, 1962</i>	
On the Thermodynamics of Surface Systems	
<i>By Jan Christer Eriksson</i>	145
<i>Manuscript received April, 1962</i>	
The Critical Region	
<i>By Marshall Fixman</i>	175
<i>Manuscript received December, 1962</i>	
The Equation of State of the Classical Hard Sphere Fluid	
<i>By H. L. Frisch</i>	229
<i>Manuscript received April, 1962</i>	
Studies in the Kinematics of Isothermal Diffusion. A Macrodynamical Theory of Multicomponent Fluid Diffusion	
<i>By Ole Lamm</i>	291
<i>Manuscript received November, 1962</i>	
Many-Electron Theory of Atoms, Molecules and Their Interactions	
<i>By Oktay Sinanoğlu</i>	315
<i>Manuscript received March, 1963</i>	
Ionic Solvation	
<i>By J. Stecki</i>	413
<i>Manuscript received April, 1962</i>	
Melting Mechanisms of Crystals	
<i>By A. R. J. P. Ubbelohde</i>	459
<i>Manuscript received April, 1962</i>	
Author Index	481
Subject Index	491

TOWARD AN ANALYTIC THEORY OF CHEMICAL REACTIONS

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CONTENTS

I. Introduction	2
II. Identification and Characterization of Species	2
A. Species Identification	3
B. Species Characterization	9
(1) Born–Oppenheimer Approximation	9
(2) Born–Oppenheimer Separation	20
III. Interaction of Species	22
A. Critical Exposition of the Semiempirical Method	25
B. Nonempirical Electronic Energy Computations	32
IV. Collision Dynamics	35
A. Separation of External Motion	35
B. First-Order Approximations	37
(1) First-Order Time-Dependent Perturbation Theory	37
(2) Scattering Cross-Section	40
(3) Born Approximation	42
(4) Rearrangement Collisions	44
(5) Application to Chemical Reactions	46
C. Better Approximate Solutions of the Time-Independent Schrödinger Equation	47
(1) Partial Waves	47
(2) Distorted Waves	49
(3) Strong Coupling	51
(4) Perturbed Stationary-State Wave Functions	52
D. Numerical Solution of the Time-Dependent Schrödinger Equation	53
V. Many-Particle Dynamics	55
A. Pauli Equation	59
B. Modified Boltzmann Equation	62
C. Quantum Statistical Formulation of the Onsager Theory	68
References	80

ELECTRON GAS IN A LATTICE OF POSITIVE CHARGES

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CONTENTS

I. Introduction	85
II. General Formalism	88
A. Expansion in Powers of the Interaction Parameter	88
B. Expansion in Powers of the Activity	93
C. Relation between the Two Kinds of Expansion	97
III. Electron Gas in a Lattice of Positive Charges	99
A. The Problem of Long-Range Forces	99
B. Elimination of Divergences of Type I	103
IV. Electron Gas in a One-Component Lattice	112
A. Limit of Zero Temperature	112
B. Evaluation of the Diagrams	113
(1) Zeroth Order	115
(2) Madelung Term	115
(3) First Order	116
(4) Second Order	117
C. Ground-State Energy in Terms of the Density	122
D. Discussion of the Results	124
E. Effect of the Structure of the Positive Charges. Modified Coulomb Potential	127
V. Multicomponent Lattices	130
A. Superlattices	130
B. Disordered Lattice	135
VI. Conclusions	142
References	143

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ON THE THERMODYNAMICS OF SURFACE SYSTEMS

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CONTENTS

I. Introduction	145
II. Physical Considerations	146
III. The Energy Differential for an Equilibrium Surface System	149
IV. Gibbs' Adsorption Law	151
V. The Energy Differential for a Nonequilibrium Surface System	153
VI. Basic Assumptions Made in Other Treatments	154
VII. The Surface Phase Treated as a Series of Homogeneous Sub-phases	158
VIII. The General Adsorption Law	160
IX. The Surface Tension of Liquid Mixtures	163
A. General	163
B. The Experimental Verification of Eq. (71)	163
C. Derivation of Szyszkowski's Formula. Traube's Rule	166
D. The Equation of State for Surface Films	167
E. Extreme Values of the Surface Tension of Binary Mixtures	168
X. Adsorption at Liquid-Gas and Liquid-Liquid Interfaces	169
A. General	169
B. Langmuir's Adsorption Formula	170
XI. Surface Equilibria	171
XII. Conclusions	172
XIII. Acknowledgements	173
References	173

THE CRITICAL REGION*

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CONTENTS

I. Introduction	175
II. The Coexistence Curve	176
A. Classical Thermodynamics	176
B. Experimental Problems	179
III. Radial Distribution Function	181
A. History	181
B. An Approximate Treatment	183
C. Summation Methods	192
IV. Light Scattering and X-Ray Diffraction	194
V. Viscosity	197
VI. Heat Capacity	207
VII. Sound Propagation	215
VIII. Miscellany	222
A. Diffusion	222
B. Sound Propagation in Gases	223
C. Viscosity and Thermal Conductivity of Gases	223
D. Dielectric Behavior	224
References	224

THE EQUATION OF STATE OF THE CLASSICAL HARD SPHERE FLUID

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CONTENTS

I. Introduction	229
II. The Statistical Description of a Simple Fluid	231
III. Review of Other Theories of Fluids	233
A. Power Series Methods	234
B. Integral Equation Methods	235
C. Lattice Theories (Hole, Cell and Free Volume Theories)	238
IV. The Hard Sphere System	240
V. The Equation of State of the Hard Sphere Fluid	253
VI. Discussion and Applications	266
References	287

STUDIES IN THE KINEMATICS OF ISOTHERMAL DIFFUSION. A MACRO-DYNAMICAL THEORY OF MULTICOMPONENT FLUID DIFFUSION

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CONTENTS

I. The Problem and the Method	291
II. General Formulation of Multicomponent Diffusion	293
III. Two Components	295
IV. Three Components	297
V. Reductions to Self Diffusion	302
VI. Details Regarding the Chemical Components as Dynamical Objects	306
VII. A Case of Non-differential Three-Component Diffusion	309
VIII. Historical Remark on the Osmotic Pressure and Diffusion	312
References	312

MANY-ELECTRON THEORY OF ATOMS, MOLECULES AND THEIR INTERACTIONS*

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CONTENTS

I. Introduction	316
II. Why a "Many-Electron" Theory?	317
III. Semi-empirical Theories	319
IV. Non-empirical Theories	320
V. Plan of the Many-Electron Theory	321
VI. Orbitals	323
VII. Antisymmetry and Relative Electron Distributions	325
VIII. Hartree-Fock Equations	327
IX. The Exact Many-Electron Wave Function	330
X. Orbital Orthogonality	335
XI. Unlinked Clusters	337
XII. Variation Principle and the Exact Energy	339
XIII. Various Correlation Effects in the Exact Wave Function and the Energy	340
XIV. Variation-Perturbation Approach	342
XV. Various Many-Particle Theories	344
A. Generalized SCF Methods	344
B. Perturbation Theory	346
C. "Many-Electron Theory"	349
XVI. The Wave Function of the "Many-Electron Theory"	349
XVII. Variational Energy of the "Many-Electron Theory"	350
XVIII. Many-Electron Correlations	353
A. Many-Electron Effects in the Wave Function	353
B. Many-Electron Effects in the Energy	357
XIX. Effect of Correlation on Orbitals, $\hat{f}_i$	358

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XX. Non-Closed Shells	363
XXI. Near-Degeneracy	366
XXII. Pair Correlations	368
XXIII. Symmetry Properties	372
XXIV. Atoms	376
XXV. Small Molecules	383
XXVI. π -Electron Systems	384
XXVII. Localization—Bonds, Lone Pairs, Ion Cores	387
A. Transformation on the Exact Energy	389
B. Transformations on the Approximate Energies	390
C. Transformations on the Variational Energies	391
D. Effect of Molecular Environment on a Bond	395
E. Calculation of a Bond Energy	396
XXVIII. Van der Waals Attractions	398
A. Intramolecular Attractions	399
B. Intermolecular Attractions	400
XXIX. Relativistic Effects	406
XXX. Conclusion	407
References	409

IONIC SOLVATION

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CONTENTS

I. Introduction	413
II. Intermolecular Potential Energy of a System of Molecules and Ions	415
A. Conventional Distinction between Types of Interaction	415
B. Potential Energy of a System of Ions and Non-polar Molecules	417
C. Potential Energy of a System of Ions and Polar Molecules	418
III. Free Energy of Charging a Set of Ions	420
A. General Relations and Potentials of the Average Force	420
B. Irreducible Interactions	422
C. Expansion in Powers of Ionic Charge	423
IV. Potential of the Average Force in a Non-polar Solvent	425
A. Derivation of the Coulomb Macroscopic Law for Two Ions	425
B. The Rigid-Lattice Model	433
V. Potential of the Average Force between Two and Three Ions in a Dipolar Solvent	435
A. Asymptotic Coulomb Law for Two Ions	435
B. Rigid-Lattice Model of Solvent Structure	436
C. Higher Powers of Ionic Charges	442
D. Irreducible Interactions between Three Ions, $w_3^{(\alpha\beta\gamma)}$	444
VI. Free Energy of Charging a Single Ion	444
A. Non-polar Solvents	445
B. Polar Solvents	449
C. Rigid Lattice of Point Non-polarizable Dipoles	451
References	458

MELTING MECHANISMS OF CRYSTALS

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CONTENTS

I. Melting and Crystal Structure	459
II. Premelting and Prefreezing Phenomena	460
III. Similitude Rules for Melting	462
IV. Critical Melting	463
V. Some Prominent Mechanisms of Melting	463
A. Positional Disorder	463
B. Rotational Disorder	466
VI. Melts for which Quasi-crystalline Models are Inadequate	467
VII. Formation of Association Complexes on Melting	469
VIII. Association Complexes in Ionic Melts	474
IX. A Conglomerate Model for Ionic Melts	476
X. Symmetry Decreases on Melting	478
References	479